No Free Lunches in Machine Learning

Neill Campbell

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Department of Computer Science, University of Bath Slide input credits: Carl Henrik Ek, Javier González, Simon Prince, Julian Faraway







AI Talks: AI & ML Research Group, Department of Computer Science

11 Oct 2023 Prof Simon Prince

Understanding Deep Learning: The Technology Behind Modern AI

15 Nov 2023 Prof Nello Cristianini

The Shortcut: How Machines Became Intelligent Without Thinking in a Human Way

13 Dec 2023 Prof Mike Tipping

The Irresistible Rise of Machine Learning

28 Feb 2024 Prof Neill Campbell

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20 Mar 2024 Prof Özgür Şimşek

Reinforcement Learning and the Pursuit of Artificial Intelligence

17 Apr 2024 Dr Harish Tayyar Madabushi

Emergent Abilities of Language Models: Do they pose an existential threat?

8 May 2024 Prof Darren Cosker

Al for Human Sensing: Research, Productisation and Ethics

TBD Prof Mike Tipping

Bayesian Inference in Machine Learning: Indistinguishable from Magic?





Overview

What questions do we have about ML?

• Can I use ML to solve x?

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- What does ML actually do?

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- Can any of this be used for science/engineering?

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No Free Lunch

Uncertainty / Error Bars

Model Selection

Causality

Conclusions

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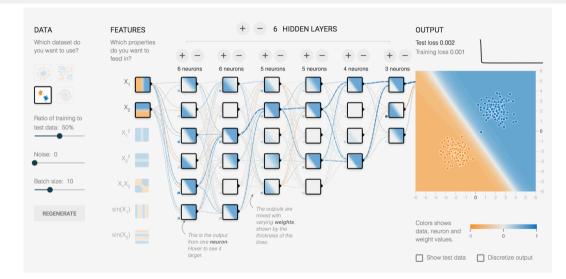
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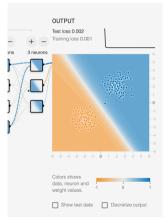
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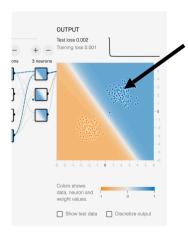
Conclusions

Neural Network Playground:

https://playground.tensorflow.org/

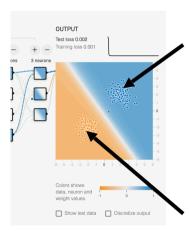










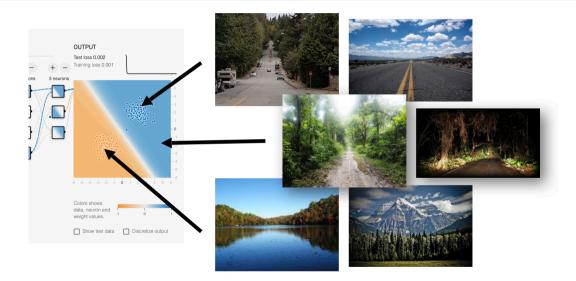






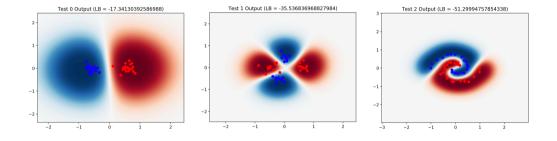




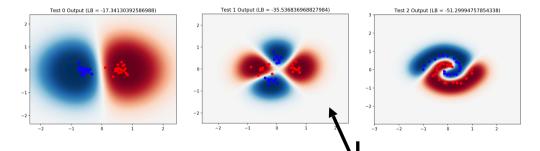


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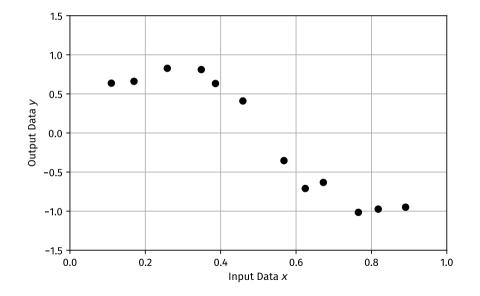


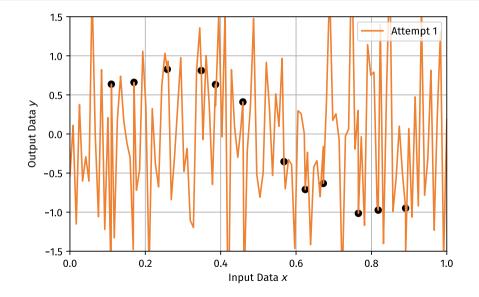


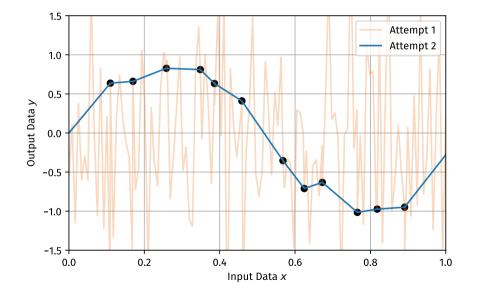
We need to consider **properties** of Machine Learning approaches

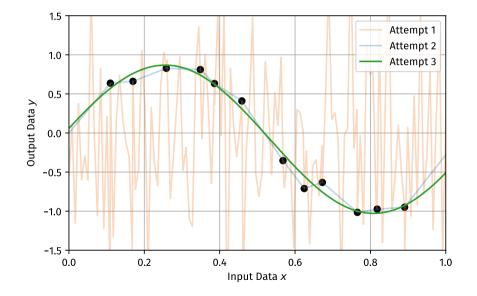
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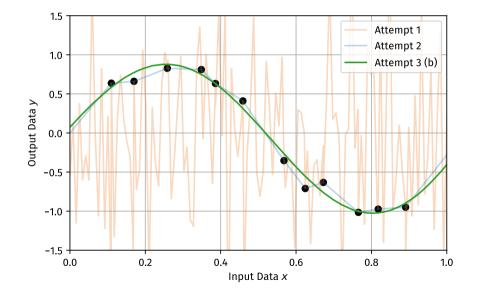
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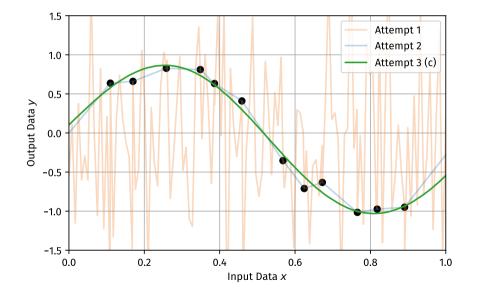


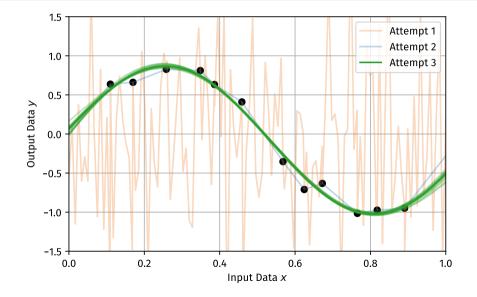


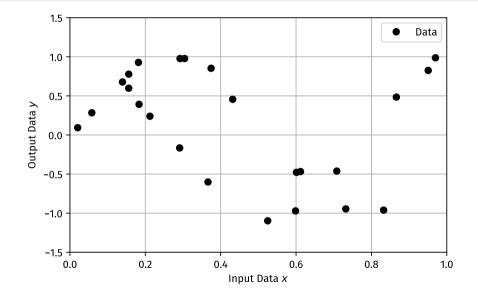


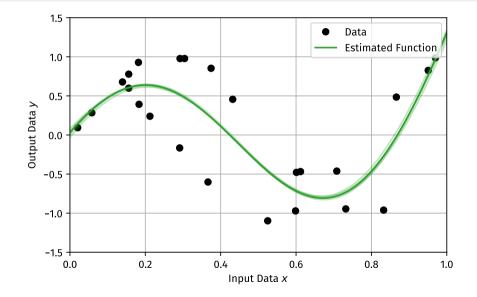


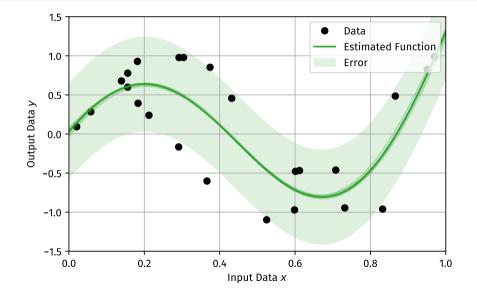


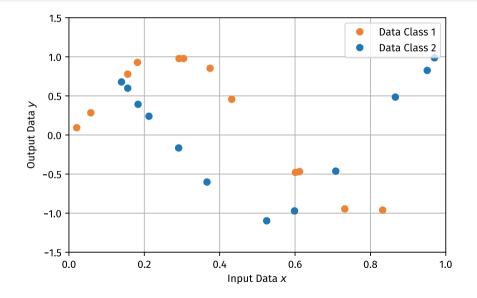


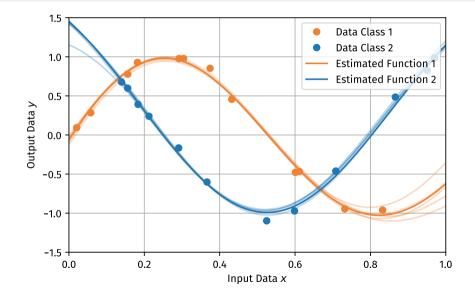


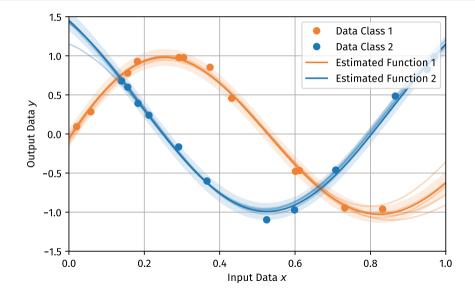


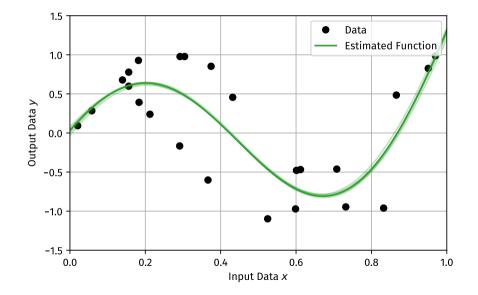


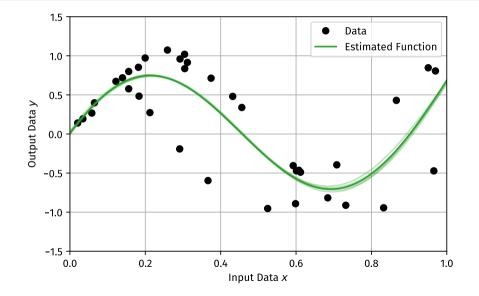


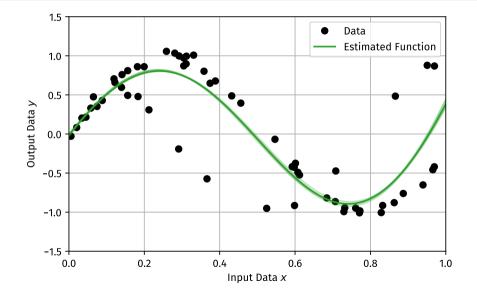


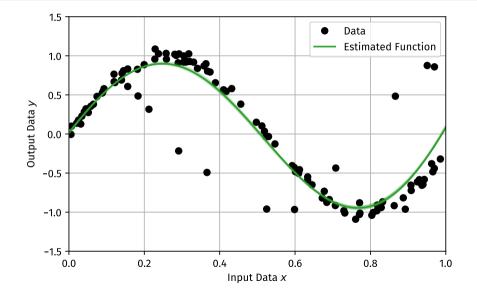




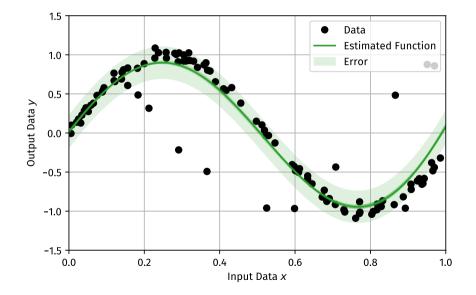




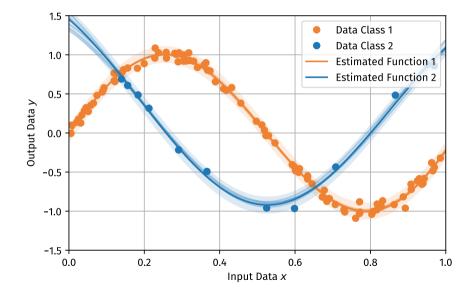




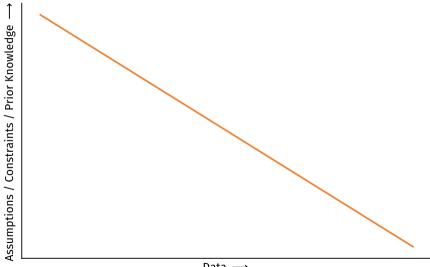
Average vs Worst Case: Failure to model..



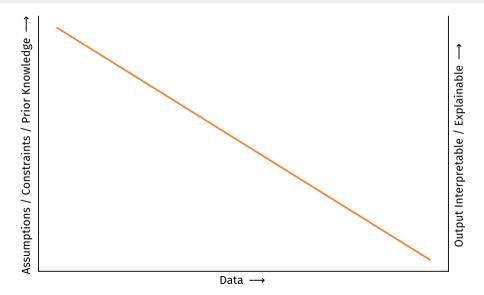
Average vs Worst Case: Explicitly accounting for imbalance..



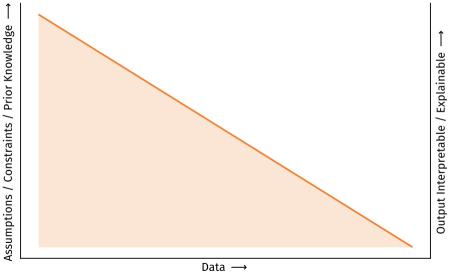
No free lunch



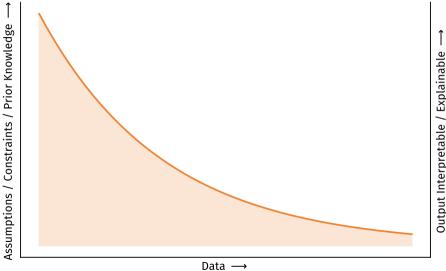
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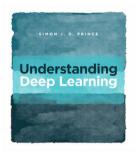


No free lunch (more realistic)



Output Interpretable / Explainable

Understanding Deep Learning



Excellent new text book from Simon Prince (visiting Prof in Bath for semester 1):

Understanding Deep Learning, Simon J.D. Prince, MIT Press

Final draft available on the website: https://udlbook.github.io/udlbook/

Uncertainty / Error Bars

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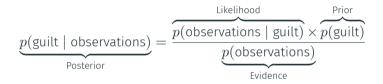
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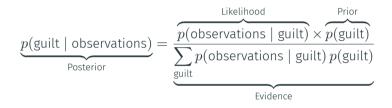
• Bayes' Rule

Posterior Probability (after) = <u>Likelihood (of event) × Prior Probability (before)</u> Evidence • Consider a legal trial..



 $p(A \mid B)$ means "probability of A being the case given that B occurs"

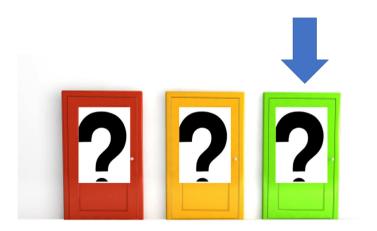
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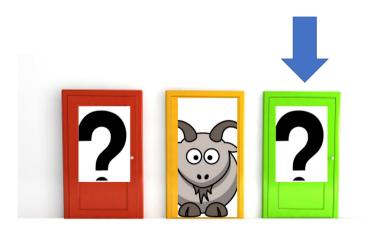


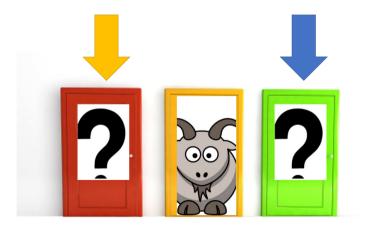
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Monty Hall: How would we generate data (or simulate)?

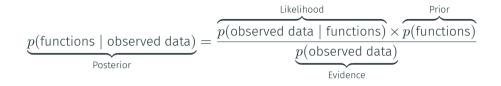
```
1 door_with_car = pick_random({1, 2, 3})
2 door_with_goat = {1, 2, 3} - door_with_car
3
4 door_picked = pick_random({1, 2, 3})
5
6 if door_picked == door_with_car:
7 door_to_open = pick_random(door_with_goat)
8 else:
9 door to open = door with goat - door picked
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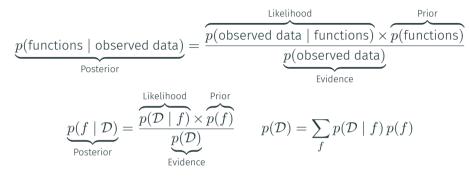
```
1 door_with_car = pick_random({1, 2, 3})  # 1/3 equal chance
2 door_with_goat = {1, 2, 3} - door_with_car
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4 door_picked = pick_random({1, 2, 3})  # 1/3 equal chance
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6 if door_picked == door_with_car:
7 door_to_open = pick_random(door_with_goat)  # 1 times in 3
8 else:
9 door to open = door with goat - door picked  # 2 times in 3
```

Consider Modelling and ML as a Generative Process

Bayes' Rule with models and functions..

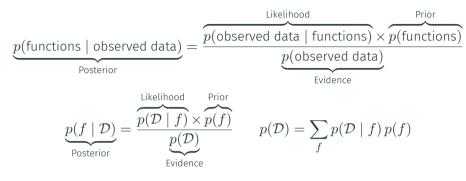


Bayes' Rule with models and functions..



Data $\mathcal{D} = \{X, Y\}$, pairs of inputs $\{x_n\}$ and outputs $\{y_n\}$, and functions f

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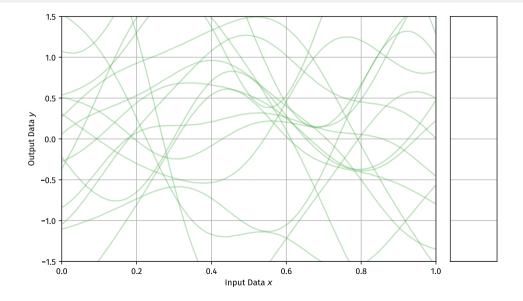


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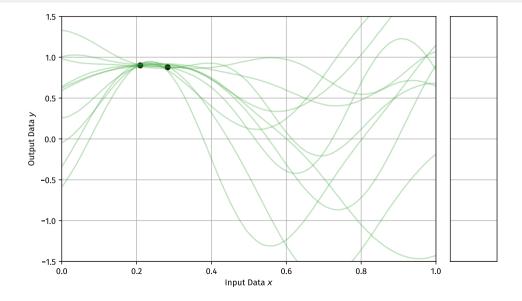
Average over functions to predict unknown output y^* for a new input x^* :

$$p(y^* \mid x^*, \mathcal{D}) = \sum_f p(y^* \mid x^*, f) \, p(f \mid \mathcal{D})$$

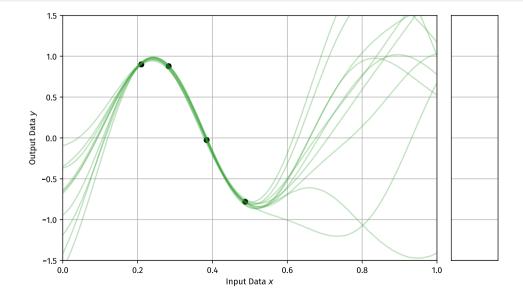
Prior over functions...



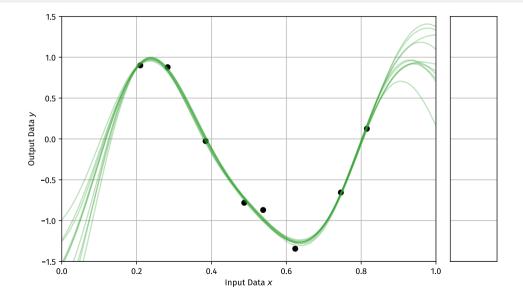
Combine prior with data...



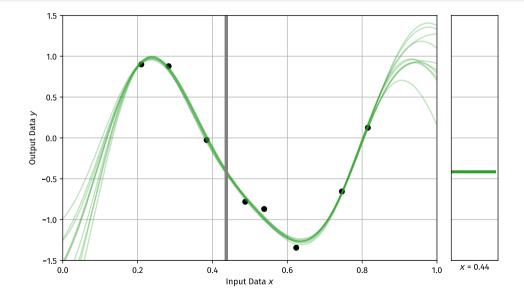
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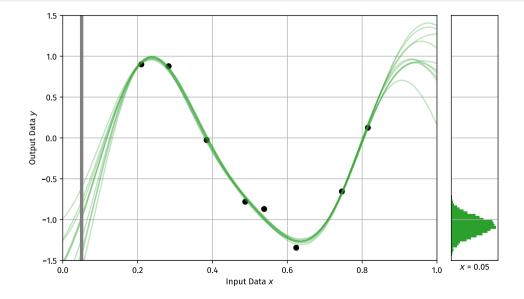
Combine prior with data...



Average over functions to predict...



Averaging over functions gives us (Epistemic) Uncertainty!



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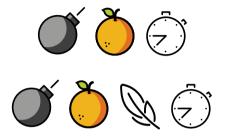
Science (and Machine Learning) cannot prove things to be true via data Science (and Machine Learning) cannot prove things to be true via data we can only demonstrate that things are inconsistent with data



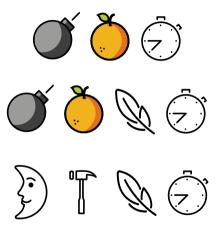














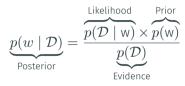
Stable Diffusion: "Drop cannonball and orange off the leaning tower of Pisa."



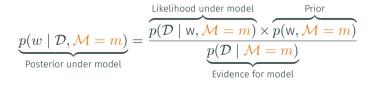
576K views 8 years ago

At the end of the last Apollo 15 moon walk, Commander David Scott (pictured above) performed a live demonstration for the television cameras. He held out a geologic hammer and a feather and dropped them at the same time. Because they were essentially in a vacuum, there w ...more

Bayes' Rule for model selection..

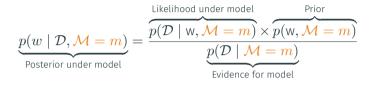


Data $\mathcal{D} = \{X, Y\}$, input/output pairs, and parameters w

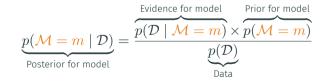


Data $\mathcal{D} = \{X, Y\}$, input/output pairs, and parameters w for Model $\mathcal{M} = m$

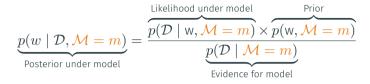
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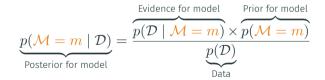
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Bayes' Rule for model selection..



Data $\mathcal{D} = \{X,Y\}$, input/output pairs, and parameters w for Model $\mathcal{M} = m$



If prior over models is equal, we compare via the Evidence for the Model: $p(\mathcal{D} \mid \mathcal{M} = m)$

Fitting polynomial models to data under Gaussian noise, $\varepsilon_n \sim \mathcal{N}(0, \sigma^2)$:

Model 1:
$$y_n = a_0 + a_1x_n + \varepsilon_n$$

Model 2: $y_n = a_0 + a_1x_n + a_2x^2 + \varepsilon_n$
Model 3: $y_n = a_0 + a_1x_n + a_2x^2 + a_3x^3 + \varepsilon_n$
Model 4: $y_n = a_0 + a_1x_n + a_2x^2 + a_3x^3 + a_4x^4 + \varepsilon_n$
Model 5: $y_n = a_0 + a_1x_n + a_2x^2 + a_3x^3 + a_4x^4 + a_5x^5 + \varepsilon_n$

Parameters $w_m = [a_0, \ldots, a_m]$ for model m, where $m \in [1, \ldots, 5]$.

Model selection example (more noise)

Causality

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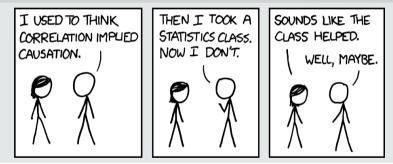
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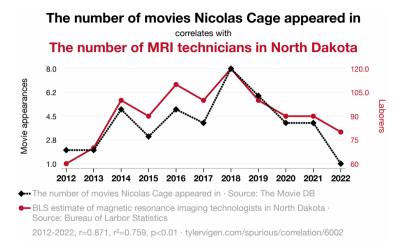
Correlation is not Causation

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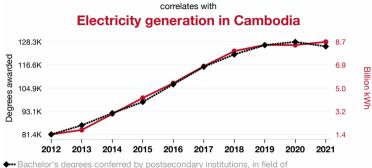


Danger Batman..



[https://tylervigen.com/spurious-correlations]





Bachelor's degrees conferred by postsecondary institutions, in field of study: Engineering · Source: National Center for Education Statistics

 Total electricity generation in Cambodia in billion kWh · Source: Energy Information Administration

2012-2021, r=0.997, r²=0.994, p<0.01 · tylervigen.com/spurious/correlation/2716

[https://tylervigen.com/spurious-correlations]

"Correlation is not Causation"

- Do we need causation?
- Is science not just correlation?

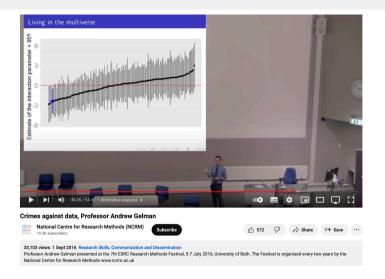
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Importance simultaneously undervalued and overestimated?

Objectivity..

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[Andrew Gelman: "Crimes against Data"]

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 - e.g. Atmospheric pressure and barometer needle reading

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An object is the cause of another ...

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[David Hume, Enquiry Concerning Human Understanding, 1748]

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 - e.g. Atmospheric pressure and barometer needle reading

Formal definitions tricky but:

An object is the cause of another ...

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• Introduces the idea of a counterfactual

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 ${\sf ACTION} \ \rightarrow \ {\sf OUTCOME}$

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• Hypothetical world:

Counterfacutal Action \rightarrow Counterfactual Outcome

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• Difference in outcome = effect of the action!

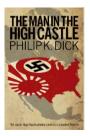
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Problems with counterfactuals..

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- Could the counterfactual possibily occur?
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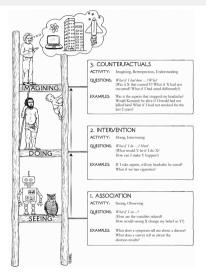
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 - Can we use ML to estimate the counterfactuals?

- We never get to observe the counterfactual :-(
- Could the counterfactual possibily occur?
 - All the time inside our heads!
 - What if I'd bought some tasty chocolates for Neill?
- Philosophical difficulties/objections..
- Can we approximate the counterfactual?
 - Lots of the time in science \rightarrow the Randomised Control Trial (RCT)!
- Exciting question: what if we can't do RCT?
 - Can we use ML to estimate the counterfactuals? Possibly!

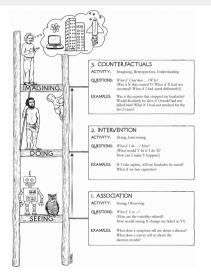
ML for Causation: Pearl's "Ladder of Causation"..

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[Pearl and Mackensie 2017]

ML for Causation: Pearl's "Ladder of Causation"..



Causal reasoning cannot be answered by data alone we will need a model as well!

[Pearl and Mackensie 2017]

• Two disease treatments (surgical/non-surgival for kidney stones)

 Positive Outcome

 Treatment A
 273/350 = 78%

 Treatment B
 289/350 = 83%

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Treatment A	273/350 = 78%	81/87 = 93%	192/263 = 73%
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• What's going on?

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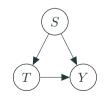
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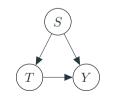


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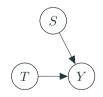
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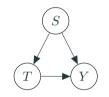


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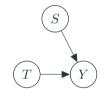


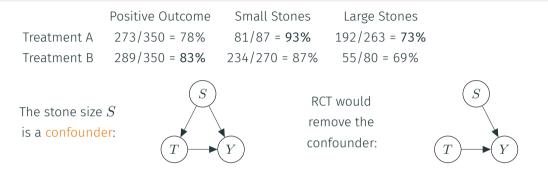
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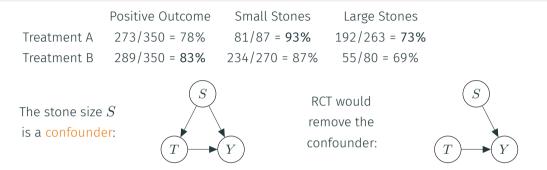


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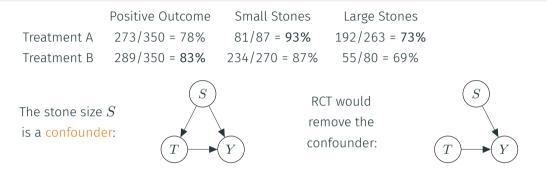


 $p(A \mid B)$ means "probability of A being the case given that B occurs" by observation alone $p(Y \mid T) = \sum_{s} p(Y \mid S, T) p(T \mid S) p(S) / p(T)$

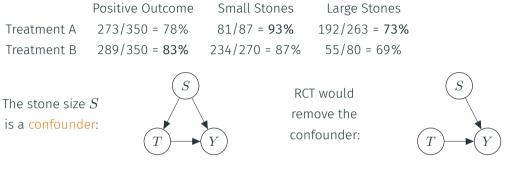


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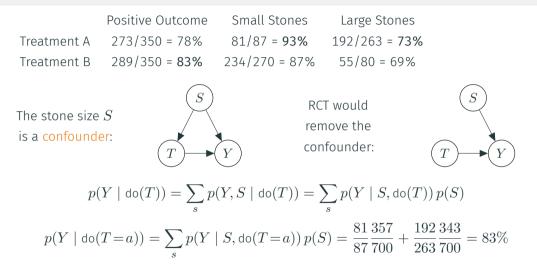
Probability of outcome Y given intervening with treatment T is $p(Y \mid \operatorname{do}(T))$

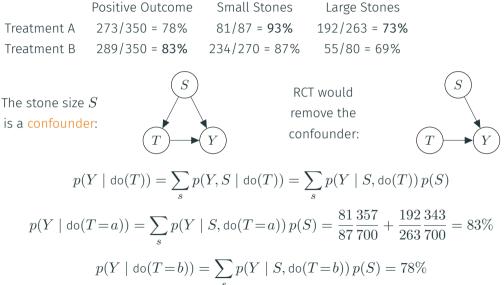


$$\begin{split} p(A \mid B) \text{ means "probability of } A \text{ being the case given that } B \text{ occurs" by observation alone} \\ p(Y \mid T) &= \sum_{s} p(Y \mid S, T) \, p(T \mid S) \, p(S) \, / \, p(T) \end{split}$$
 $\begin{aligned} \text{Probability of outcome } Y \text{ given intervening with treatment } T \text{ is } p(Y \mid \text{do}(T)) \\ p(Y \mid \text{do}(T)) &= \sum_{s} p(Y, S \mid \text{do}(T)) = \sum_{s} p(Y \mid S, \text{do}(T)) \, p(S) \end{aligned}$



$$p(Y \mid \operatorname{do}(T)) = \sum_{S} p(Y, S \mid \operatorname{do}(T)) = \sum_{S} p(Y \mid S, \operatorname{do}(T)) p(S)$$





- Statistical/Probabilistic reasoning alone cannot support causal inference
- Determining the joint probability distribution of variables says nothing about causation
- **Causal Inference:** promises to determine the necessary set of (non-data) assumptions sufficient to make a causal conclusion

[Thanks to Julian Faraway for Causal Illustrations]

Overview...

Overview

No Free Lunch

Uncertainty / Error Bars

Model Selection

Causality

Conclusions

Did we answer any of the questions?

- Can I use ML to solve x?
- What does ML actually do?
- \cdot Isn't ML just the same as y?
- Can I replace myself/my research team with ML?
- How much data do I need?
- Can I just use Deep Learning/Generative AI/ChatGPT?
- Surely Deep Learning/Generative AI/ChatGPT is all hype?
- Can any of this be used for science/engineering?

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 - $\cdot\,$ e.g. have loads of data that spans the space
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- Need data efficiency / care about uncertainty
 - e.g. clinical/safety applications
 - \cdot Need a Bayesian method
- Want to analyse scientific results
 - e.g. does my new model explain dark matter
 - Need causal inference

• ...

Loads of gotchas..

- Availability (using the data you have not the data you need)
- Evaluation measure (is a human baseline sensible?)
- Ignore uncertainty/error bars
- Sample / dataset bias
- Bias / variance trade-off
- Haven't spoken about Decision Theory
- Lots to talk about regarding Causality
- "All models are wrong but some models are useful"

That's all folks..

AI Talks: AI & ML Research Group, Department of Computer Science

11 Oct 2023 Prof Simon Prince

Understanding Deep Learning: The Technology Behind Modern AI

15 Nov 2023 Prof Nello Cristianini

The Shortcut: How Machines Became Intelligent Without Thinking in a Human Way

13 Dec 2023 Prof Mike Tipping

The Irresistible Rise of Machine Learning

28 Feb 2024 Prof Neill Campbell

No Free Lunches in Machine Learning

20 Mar 2024 Prof Özgür Şimşek

Reinforcement Learning and the Pursuit of Artificial Intelligence

17 Apr 2024 Dr Harish Tayyar Madabushi

Emergent Abilities of Language Models: Do they pose an existential threat?

8 May 2024 Prof Darren Cosker

Al for Human Sensing: Research, Productisation and Ethics

TBD Prof Mike Tipping

Bayesian Inference in Machine Learning: Indistinguishable from Magic?